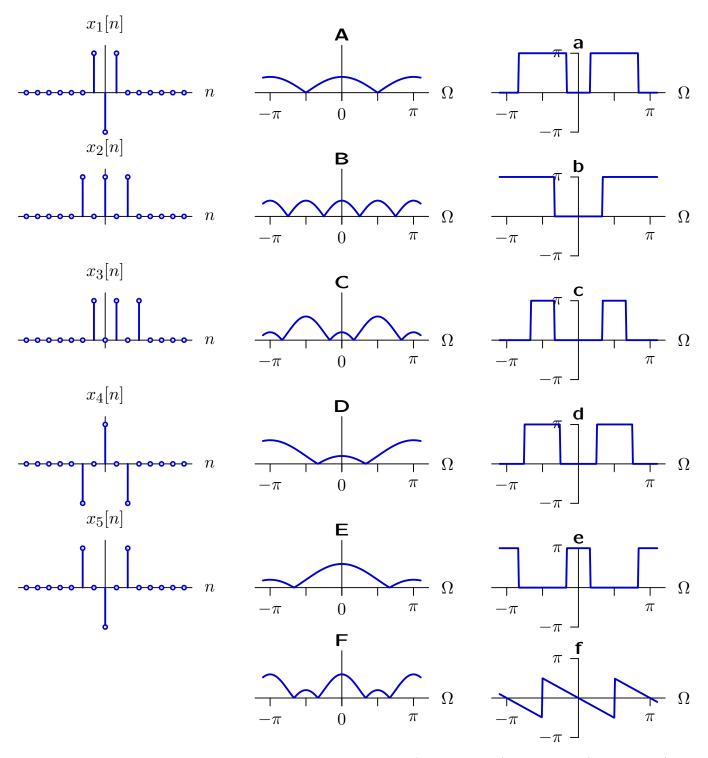
## **Fourier Transforms**

The diagrams below show five DT signals ( $x_1$  through  $x_5$ ), six DTFT magnitude plots (labeled **A** through **F**), and six DTFT angle plots (labeled **a** through **f**).



For each signal in the left column, identify its magnitude (A-F or none) and angle (a-f or none).

**Part 1.**  $X_1(\Omega) = 2\cos(\Omega) - 1$ 

magnitude: D

angle: b

**Part 2.**  $X_2(\Omega) = 2\cos(2\Omega) + 1$ 

magnitude: F

angle: c

## Part 3.

 $x_3[n] = x_2[n-1]$  $X_3(\Omega) = X_2(\Omega)e^{-j\Omega}$ 

We also have  $\angle X_3(\Omega) = \angle X_2(\Omega) - \Omega$ . So we are looking for a phase that is linearly decreasing as  $\Omega$  increases. Graph f almost looks right (the phase is linear in  $\Omega$ ), but it doesn't have jumps by  $\pm \pi$  at the same points that graph c does, so the correct answer is none.

magnitude: F

angle: none

**Part 4.**  $X_4(\Omega) = 1 - 2\cos(2\Omega)$ 

magnitude: C

angle: e

**Part 5.**  $x_5[n] = -x_4[n]$ 

 $X_1(\Omega) = -X_3(\Omega)$ 

Thus, its magnitude should be the same as  $|X_2(\Omega)|$ , and its phase graph should have the same rough shape as  $X_4$ 's, but with 0 and  $\pi$  swapped.

magnitude: C

angle a